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<p>(21) International Application Number: PCT/US99/26554</p> <p>(22) International Filing Date: 9 November 1999 (09.11.99)</p> <p>(30) Priority Data: 60/107,879 9 November 1998 (09.11.98) US</p> <p>(71) Applicant (for all designated States except US): BROADCOM CORPORATION [US/US]; 16215 Alton Parkway, Irvine, CA 92618 (US).</p> <p>(72) Inventor; and (75) Inventor/Applicant (for US only): CAMERON, Kelly, B. [US/US]; 4171 Black Fin Avenue, Irvine, CA 92620 (US).</p> <p>(74) Agent: O'ROURKE, John, F.; Christie, Parker & Hale, LLP, P.O. Box 7068, Pasadena, CA 91109-7068 (US).</p>		<p>(81) Designated States: AL, AM, AT, AU, AZ, BA, BB, BG, BR, BY, CA, CH, CN, CR, CU, CZ, DE, DK, DM, EE, ES, FI, GB, GE, GH, GM, HR, HU, ID, IL, IS, JP, KE, KG, KP, KR, KZ, LC, LK, LR, LS, LT, LU, LV, MA, MD, MG, MK, MN, MW, MX, NO, NZ, PL, PT, RO, RU, SD, SE, SG, SI, SK, SL, TJ, TM, TR, TT, TZ, UA, UG, US, UZ, VN, YU, ZW, ARIPO patent (GH, GM, KE, LS, MW, SD, SL, SZ, TZ, UG, ZW), Eurasian patent (AM, AZ, BY, KG, KZ, MD, RU, TJ, TM), European patent (AT, BE, CH, CY, DE, DK, ES, FI, FR, GB, GR, IE, IT, LU, MC, NL, PT, SE), OAPI patent (BF, BJ, CF, CG, CI, CM, GA, GN, GW, ML, MR, NE, SN, TD, TG).</p> <p>Published With international search report. Before the expiration of the time limit for amending the claims and to be republished in the event of the receipt of amendments.</p>
<p>(54) Title: FORWARD ERROR CORRECTOR</p>		
<p>(57) Abstract</p> <p>A method for decoding an algebraic-coded message including determining a discrepancy indicator; determining an error locator polynomial according to a modified Berlekamp-Massey algorithm such that an uncorrectable message is detected; and producing a perceptible indication of the detected uncorrectable message. An apparatus includes storage devices, arithmetic components, and an uncorrectable message detector.</p> <div data-bbox="790 1094 1417 1921"> <pre> graph TD BEGIN([BEGIN]) --> INIT[INITIALIZE 21] INIT --> F2t{F=2t? 22} F2t -- YES --> UPDATE_EL[UPDATE ERROR LOCATOR 23] F2t -- NO --> EQ4[EQ. 4 24] EQ4 --> EQ5[EQ. 5 25] EQ5 --> STRONG{Strong enough? 29} STRONG -- YES --> EQ6a[EQ. 6a 27] STRONG -- NO --> EQ6b[EQ. 6b 28] EQ6a --> UPD_AUX[Update Auxiliary Polynomial] EQ6b --> UPD_AUX UPD_AUX --> UPD_CTRL[Update Controller State] UPD_CTRL --> STATE0{STATE = 0?} STATE0 -- YES --> STATE1[STATE = 1] STATE0 -- NO --> DEL0{DEL = 0?} DEL0 -- YES --> PWL1[PWL = PWL + 1] DEL0 -- NO --> PWL1 PWL1 --> PWL2[PWL = PWL - 1] PWL2 --> INC_T[INCREMENT T=t+1 22] INC_T --> F2t F2t --> END([END]) </pre> <p style="text-align: right;">mBM ALGORITHM</p> </div>		

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1 FORWARD ERROR CORRECTOR

CROSS-REFERENCE TO RELATED APPLICATION

5 This patent application claims the benefit of the filing date of U.S. Provisional Patent Application Serial No. 60/107,879, filed November 9, 1998 and entitled FORWARD ERROR CORRECTOR, the entire contents of which are hereby expressly incorporated by reference.

BACKGROUND OF THE INVENTION

1. Field of the Invention

10 The present invention relates to an apparatus for correcting errors present in stored or transmitted data; and, more particularly, to an apparatus for evaluating an error evaluator polynomial, an error locator polynomial and a differential polynomial which are used in correcting errors in the data encoded by using an algebraic code, such as a Reed-Solomon code.

15 2. Description of Related Art

Noise occurring during a process of transmitting, storing or retrieving data can in turn cause errors in the transmitted, stored or retrieved data. Accordingly, various encoding techniques, having the capability of rectifying such errors, for encoding the data to be transmitted or stored have been developed.

20 In such encoding techniques, a set of check bits is appended to a group of message or information bits to form a codeword. The check bits, which are determined by an encoder, are used to detect and correct the errors. In this regard, the encoder essentially treats the bits comprising the message bits as coefficients of a binary message polynomial and derives the check bits by multiplying the message polynomial $R(x)$ with a code generator polynomial $G(x)$ or
25 dividing $R(x)$ by $G(x)$, to thereby provide a codeword polynomial $C(x)$. The code generator polynomial is selected to impart desired properties to a codeword upon which it operates so that the codeword will belong to a particular class of error-correcting binary group codes (see, e.g., S. Lin et al., "Error Control Coding: Fundamentals and Applications", Prentice-Hall, 1983).

30 One class of error correcting codes is the well-known BCH (Bose-Chaudhuri-Hocquenghen) codes, which include the Reed-Solomon ("RS") code. The mathematical basis of the RS code is explained in, e.g., the aforementioned reference by Lin et al. and also in Berlekamp, "Algebraic Coding Theory", McGraw-Hill, 1968, which is further referred to in U.S. Pat. No. 4,162,480 issued to Berlekamp. The aforementioned references are hereby incorporated by reference in pertinent part.

35 SUMMARY OF THE INVENTION

The invention herein provides a method and apparatus for decoding an algebraic-coded message. The method can include the steps of determining a discrepancy indicator, with the

1 discrepancy being between a calculated and a predicted value; determining an error locator
polynomial using a selected class of error correction algorithms, such as, for example, a
Berlekamp-Massey algorithm; and detecting an uncorrectable message using the selected error
5 correction algorithm. The apparatus is composed of storage devices which can include
recirculating storage devices; arithmetic components attached to the storage devices, the
components operating over a Galois Field on selected contents of the storage devices; and an
uncorrectable message detector, connected with the storage devices and the arithmetic
components.

10 BRIEF DESCRIPTION OF THE DRAWINGS

Figure 1 is an illustration of an algebraic decoder according to the invention herein;

Figure 2 is a data flow diagram of a modified Berlekamp-Massey algorithm according to
the invention herein;

Figure 3 is a block diagram illustrative of an exemplary embodiment of the present
15 invention;

Figure 4 is a block diagram of a circular syndrome generator according to the present
invention; and

Figure 5 is a block logic diagram of a logic register which can be used in the circular
syndrome generator illustrated in Figure 4.

20

EXEMPLARY EMBODIMENTS OF THE INVENTION

The invention herein provides an apparatus for and a method of decoding algebraic codes,
including BCH codes, and more specifically, Reed-Solomon codes, such that uncorrectable
messages, or portions of received encoded data, are detected. Furthermore, the invention herein
25 provides for a more area-efficient device implementation of the aforementioned method. For the
purposes of illustration, the present invention will be described in terms of a subset of the BCH
codes, namely Reed-Solomon (RS) codes.

The Reed Solomon (RS) encoding technique appends to each block of k user data
symbols $2t$ redundancy symbols to create an encoded message block (where t represents the
30 designed symbol error correcting capacity of the code). These $2t$ symbols, or elements, are
selected from the Galois Field to be the roots of the generator polynomial. Therefore, there are
 $k+2t$ symbols in a RS-encoded message block. The entire message block is viewed as a
polynomial and evaluated as a polynomial at some Galois Field element. The Galois Field
element at which the polynomial is evaluated will be located at one roots of the generator
35 polynomial that are used to create the RS code. The RS code views the n -bit symbols as elements
of a Galois Field ($GF(2^n)$). A Galois field is a finite field, the elements of which may be
represented as polynomials in a , where a is a root of an irreducible polynomial of degree n . The
RS codeword consists of a block of n -bit symbols. Typically, $n = 8$ and the 8-bit symbols are

1 referred to as bytes. Constructing the Galois field $GF(2^n)$ requires a defining polynomial $F(x)$ of degree n . In addition, a primitive element β is chosen so that every nonzero element of $GF(2^n)$ is a power of β . The element β is not necessarily a root of $F(x)$.

5 A RS codeword C is viewed as a polynomial $C(x)$ and the redundancy symbols are chosen so that the roots of $C(x)$ include the roots of a generator polynomial $G(x)$ whose roots are $2t$ consecutive powers of β . The k user data symbols are viewed as the high order coefficients of a degree $k+2t-1$ polynomial, and the redundancy symbols are the coefficients of the remainder when this polynomial is divided by $G(x)$.

10 The process of corrupting the original code block $C(x)$ with errors can be viewed as adding an error polynomial $E(x)$ to $C(x)$. The resultant corrupted polynomial is known as the received polynomial $R(x)$, where $R(x)=C(x)+E(x)$. The v non-zero terms of the error polynomial contain the necessary information to completely reconstruct the original data $C(x)$, since each term corresponds to a symbol error location and magnitude.

15 Typically, RS decoding is a tripartite analysis: (1) syndrome computation; (2) solution of the error magnitude and locator polynomials; and (3) error location and magnitude estimation by respective implementations of, for example, a Chien search and the Forney algorithm. The syndromes contain error information divorced from the actual information that is intended to be analyzed for errors. The error locator polynomial provides information regarding the location of an error in the received signal, and the magnitude of the error can be determined by using both
20 the magnitude and the locator polynomials.

The thrust of the RS error correction procedure is to reconstruct the error polynomial $E(x)$. Three polynomials are used to correct a received polynomial $R(x)$: $S(x)$, a syndrome polynomial; $\Lambda(x)$, an error locator (or error location) polynomial; and $M(x)$ an error magnitude polynomial. The syndromes are computed by evaluating the polynomial $R(x)$ at all roots of $G(x)$. These values
25 are called syndromes and the syndrome polynomial $S(x)$ has these values as coefficients. The syndrome polynomial $S(x)$ is used to determine the existence of errors. The error locator polynomial $\Lambda(x)$ and the error magnitude polynomial $M(x)$ are computed from $S(x)$ by a key equation solver. The roots of the error locator polynomial $\Lambda(x)$ indicate positions in the data that are erroneous and both the error locator polynomial $\Lambda(x)$ and the error magnitude polynomial
30 $M(x)$ are used to determine the true values of the erroneous data.

Two frequently-used RS error correction algorithms are the Berlekamp-Massey and the Euclid algorithms. The present invention recasts the Berlekamp-Massey algorithm such that the inversion process typically associated with the traditional Berlekamp-Massey (tBM) algorithm is eliminated. This is important because the inversion process includes determining the
35 reciprocal of certain Galois field elements using division. Division is a time consuming arithmetic operation, the implementation of which can occupy needed component area in a device design. Therefore, the present invention can be particularly advantageous where area-efficient layout of a decoder device is desirable.

1 For further elaboration of the decoding process over Galois fields, including tBM, Chien searching, and Forney's Algorithm, see *Theory and Practice of Error Control Codes* by Richard E. Blahut (Addison-Wesley, 1983) which is incorporated by reference in pertinent part herein.

5 Figure 1 illustrates an implementation of this algorithm, in which a raw received signal 1 is directed to RS decoder unit 2 that is used to determine the error locations and error values.

Signal 1 is provided to syndrome generator 3 and delay unit 4. In syndrome generator 3, the several syndromes 5 associated with the selected encoding are derived and transmitted to polynomial solver 5. The syndrome generator 3 calculates one syndrome for each of the $2t$ roots of $G(x)$. Polynomial solver 6 utilizes the syndromes to determine the coefficients of the error location polynomial $A(x)$ 7 and the coefficients of the error magnitude polynomial $M(x)$ 8, which in turn are transmitted to error estimator 9. Estimator 9 calculates error signal 10 which is combined in summer 11 with delayed raw received input 12 to provide corrected data 13. Estimator 9 can include Chien search unit 14 which utilizes the error location polynomial $A(x)$ to search for the roots of the error locator polynomial, r_1, \dots, r_v . Typically, the Chien search unit 15 14 employs a root finding technique which involves evaluating the error locator polynomial at all elements in the field $GF(2^n)$. The roots of the error locator polynomial r_1, \dots, r_v determine the error locations. The error values are then determined using Forney's algorithm unit 15. The delayed raw received input 12 is then corrected using the output of the Forney algorithm unit 15 and the raw received input which is transmitted by delay unit 4.

20 Traditionally, the Berlekamp-Massey (tBM) algorithm, which usually is realized in polynomial solver 6 can be described by:

$$\Delta_r = \sum_{j=0}^{n-1} \Lambda_j^{(r-1)} S_{r-j} \quad (1)$$

25

$$L_r = \delta_r (r - L_{r-1} + (1 - \delta_r) L_{r-1}) \quad (2)$$

30

$$\begin{bmatrix} \Lambda^{(r)}(x) \\ B^{(r)}(x) \end{bmatrix} = \begin{bmatrix} 1 & -\Delta_r x \\ \Delta_r^{-1} \delta_r & (1 - \delta_r) x \end{bmatrix} \begin{bmatrix} \Lambda^{(r-1)}(x) \\ B^{(r-1)}(x) \end{bmatrix} \quad (3)$$

$r=1, \dots, 2t$ where $\delta_r = 1$ if both $\Delta_r \neq 0$ and $2L_{r-1} \leq r-1$, and otherwise $\delta_r = 0$. Then $\Lambda^{(2t)}(x)$ is the smallest-degree polynomial with the properties that $\Lambda_0^{(2t)}=1$, and

35

$$S_r + \sum_{j=1}^{n-1} \Lambda_j^{(2t)} S_{r-j} = 0 \quad r = L_{2t} + 1, \dots, 2t$$

where initial conditions are $\Lambda^{(0)}(x)=1$, $B^{(0)}(x)=1$, and $L_0=0$.

It is evident that the inversion indicated in Eq. 3 requires a division operation.

1 The tBM algorithm is capable of properly decoding messages that can be decoded properly, however if there is an uncorrectable case which is detectable as being uncorrectable, the uncorrectable error may be undetected and the message decoded as if it did contain a correctable error. Many times, this improperly decoded message can create additional difficulties
5 because the error may propagate through other processes in the system which employs tBM.

According to the invention herein, the modified Berlekamp-Massey (mBM) can be described by the following equations:

$$10 \quad \Delta_i = \sum_{j=1}^{2i} \Lambda_{i-1}^{j-1} S^{i-j} \quad (4)$$

$$\Lambda_i = \Delta_- \Lambda_{i-1} + x \Delta_i B_{i-1} \quad (5)$$

$$15 \quad B_i = \begin{cases} \Lambda_{i-1} & \Delta_- = \Delta_i \\ x B_{i-1} & \end{cases} \quad (6a)$$

$$(6b)$$

where: $\Delta \neq 0$

$$B_0 = 1$$

$$\Delta_i = 1$$

20

Utilization of mBM for RS decoding can be advantageous because: (1) inversion is eliminated; (2) the control structure associated with the mBM algorithm is simplified relative to that of tBM; and (3) the termination conditions of tBM are modified such that if the code is uncorrectable, errors otherwise undetected by tBM, are detected and flagged as such.

25 One implementation of the mBM algorithm is as follows, as represented in Pascal code:

```

PROCEDURE FindLocatorBMC( VAR Syndrome,Locator:Polynomial; VAR OK:BOOLEAN );
VAR  Cnt: 0..MaxParitySyms-1;           { Loop Index }
    Pwr: 0..MaxParitySyms;               { Power Counter }
    State: (Alpha,Beta);                 { State Machine State }
    Deg: INTEGER;                        { Degree }

    Del, Del0: Words;                    { Discrepancies }
    J: INTEGER;                          { Del Index }

    TempPoly: Polynomial;                { Temporary Polynomial }
    B : Polynomial;                      { Secondary Polynomial }

35 BEGIN                                { BEGIN FindLocatorBMC }
    B.L. := 0; B.D [0] :=1;              { Initial B }
    Locator.L := 0; Locator.D [0] :=1;   { Initial Locator Poly }
    Deg := 0; Pwr := 0; Del0 := 1;        { Cntr Initialization }
    State := Alpha;                      { Machine State }

```

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1      FOR Cnt := ParitySyms-1 DOWNT0 0 DO BEGIN      { Algorithm Loop      }
      Del := 0;                                       { Calculate Del      }
      FOR J := 0 TO LOCATOR.L DO
      IF Syndrome.L >= (ParitySyms-1-Cnt-J) THEN
      Del:= Add( Del, Multiply( Locator.D[J],Syndrome.D[ParitySyms-1-Cnt-J]));
5
      TempPoly :=                                     { Do Common Update      }
      PolyAdd( WordTimes( Locator, Del0 ), PolyShift( WordTimes( B, Del ), 1 ));

      IF (State=Alpha) AND (Del<0) THEN BEGIN      { Do Step A      }
      { writeln( stderr, ' B<-L' );}
      B := Locator;
      Del0 := Del
10      END                                           { Do Step A      }

      ELSE BEGIN                                     { Do Step B      }
      { writeln( stderr, ' B<-xB' );}
      B := PolyShift( B, 1 )
      END;                                           { Do Step B      }

15      IF State=Alpha THEN BEGIN                   { State is Alpha      }
      IF Del=0 THEN Pwr := Pwr +1                  { Increment Power Cntr }
      ELSE State := Beta                           { Update Next State    }
      END                                           { State is Alpha      }

      ELSE BEGIN                                     { State is Beta      }
      Deg := Deg+1;
20      IF Pwr = 0 THEN State := Alpha              { Update Next State    }
      ELSE Pwr := Pwr-1                             { Decrement Power Cntr }
      END;                                           { State is Beta      }

      Locator := TempPoly                           { Update Locator      }
      END;                                           { Algorithm Loop      }

25      Locator := PolyDenormalize( Locator, Deg);   {Update Locator Degree  }
      OK := State=Alpha
      END;                                           { END FindLocatorBMC   }

```

Often, when a forward error corrector properly detects an uncorrectable error, the existence of such an error usually is verified in a process by which the syndrome polynomials are recomputed. This approach can carry a substantial penalty relative to the process efficiency. Instead, an embodiment of the invention herein, having an improved control structure, verifies the existence of an uncorrectable error by checking the state of polynomial solver 6 at the end of the polynomial solving process.

Figure 2 exemplifies an embodiment of the process 20 implementing the aforementioned improved control structure in the context of the mBM algorithm recited in Equations 4, 5, and 6(a)-(b). Although the implementations described herein are postured for standard RS codes having a block length of, for example, 255 elements, such implementations also may be used in the context of extended Reed-Solomon codes which, in the example herein, would have 256

1 elements in the message block, i.e., have 256 elements in associated the Galois Field. It is
desirable that, in step 21, the control variables DEG, PWR, and STATE, as well as error locator
variables be initialized. It further is desirable to iterate through steps 23, 24, 25, and 26, $2t$
5 times, where $2t$ is the number of syndrome polynomials to be evaluated, and t is the error
correcting capability of the preselected code. Thus, at step 22, a counter tracking the number
of completed iterations is employed. No additions or subtractions are needed in implementing
the control variables, and only count up or down functions are used. Step 23 essentially
implements Equation 4, in which the discrepancy value DEL, associated with a particular
iteration, is determined. Similarly, step 24 implements Equation 5 in which the error locator
10 polynomial is updated. In step 25, auxiliary polynomial B , is updated according to Equation 6a
in substep 27, or Equation 6b in substep 28, based on conditions determined by logic 26. For
logic 29, it is desirable for both $STATE = ALPHA$ AND $DEL \neq zero$ to direct the data flow
via an implementation of Equation 6a in substep 27; otherwise substep 28 is used,
implementing Equation 6b. Unlike the tBM algorithm where the polynomial shift term
15 $(1 - \delta_r)x$ in Equation 3 has been normalized, the mBM algorithm does not require
normalization, avoiding an inversion/division operation. After the auxiliary polynomial is
updated in step 25, the controller state is updated in step 26.

In general, the degree of the error locator polynomial is tracked by DEG, which is an
upcounter descriptive of the true degree of the error locator polynomial and, thus, the number
20 of errors in the message block. It also is desirable to construct an error locator polynomial who
roots equate to the locations of an error. Essentially, process 20 attempts to synthesize a linear
feedback shift register (LFSR) that predicts the values of the syndrome polynomial. Such a
LFSR can be useful to find the error locations. Discrepancy value, DEL, then exposes a
discrepancy between the predicted value of the syndrome polynomial, and the value of the
25 current syndrome polynomial, and invites further processing to discover the location of the
errors. PWR is a counter that keeps track of the number of times that the controller previously
remained in $STATE = ALPHA$. It is desirable to have the STATE remain in control state
BETA for a count equivalent to the number of times that STATE previously remained in control
state ALPHA.

30 For the purposes of the invention herein, STATE can be used to (1) determine whether
the error correction analysis ought to follow the flow of Equation 6a or 6b; (2) assist in
determining whether the degree of the error locator polynomial ought to be increased; and (3)
whether there exists an uncorrectable error. At the end of $2t$ iterations, the value of STATE is
once again determined at step 35. If the result is $STATE = ALPHA$, then the code is potentially
35 valid; on the other hand, if $STATE = BETA$, then the error is flagged as uncorrectable.
Potentially valid codes where $STATE = ALPHA$ at step 35, also can be subjected to additional
validation before being subsequently decoded. Indeed, in one subsequent operation, the number

1 of the error locator polynomial zeroes is compared with the value of DEG. A discrepancy between these two values also is indicative of an uncorrectable error.

Figure 3 is an exemplary embodiment of a polynomial solver using the mBM algorithm. Solver 50 can include syndrome generator register 51, recirculating syndrome register 52, first delay register 53, locator polynomial (Λ_i) register 54, auxiliary polynomial (B_i) register 55, second delay register 56, first multiplier 57, second multiplier 58, adder 59, Δ register 60, and Δ register 61. In another embodiment, syndrome generator 51 can be separate from solver 50. It is desirable for multipliers 57, 58, and adder 59 to operate on Galois Field elements. It also is desirable for register 51 to be logically arranged as a circular register or loop, such that particular register values can be used in a pre-defined sequence. Furthermore, it is desirable that registers 52, 54, and 55 be logically arranged as push-down stacks or FIFOs, and also that the values contained therein rotate synchronously. The error locator polynomial Λ_i are arranged in register 54 such that the least significant coefficient is at the top and the stack "grows down" as subsequent values are determined. It is desirable for the syndrome recirculating register 52 to operate such that the least significant coefficient is aligned with the bottom of the register, and the most significant with the top.

In the example of Figure 3, the error correcting capability, t , is selected to be 5 elements and, thus, syndrome register 51 is designed to employ $2t$, or 10, individual elements. Additionally, register 52 is selected to use t elements, register 54 is chosen to employ $t+1$ elements, and register 55 is intended to operate with t elements.

Initially, recirculating syndrome register 52 is pre-loaded with zeroes. As expressed in the aforementioned algorithm, an initial step involves calculating the discrepancy value DEL, which can be stored in register 60. A previous value for DEL, DEL0, is provided in register 61. To calculate the initial value for DEL, first syndrome value S_0 is shifted into register 52, which value is received in first multiplier 57 along with the initial value of DEL, namely, DEL0, and the t -th value in locator polynomial register 54. After the indicated multiplication and creation of a DEL value, the values in registers 52, 54, and 55 are shifted down by one element. At first, the values in register 52 are zero, however, with subsequent clocking, successive values of S_i enter register 52 and are recirculated therethrough, for the clock cycles equivalent to $i = 0$ to $2t-1$. As S_0 exits register 52 into first multiplier 57, corresponding values of Λ_0 are also transmitted to first multiplier 57 such that the value $S_0 \Lambda_0$ is determined.

Concurrently with this calculation, value B_0 from register 55 is multiplied with then extant value for DEL in second multiplier 58 and the result is summed with $S_0 \Lambda_0$ in adder 59 to produce the next value for DEL. This value of DEL is used to produce the next value for the error locator polynomial, namely, Λ_1 . After this calculation, value S_0 is recirculated such that it bypasses first delay register 53 and re-enters recirculating register 52 at the top of the stack during the next clock cycle. During this next clock cycle, syndrome value S_1 is aligned, and multiplied, with Λ_0 , and S_0 is aligned, and multiplied, with Λ_1 . This process repeats such that

1 each of the syndrome values properly iterates through in the evaluation of the locator polynomial.

With the above information, a skilled artisan would be able to see the manner in which the values for error locator polynomial Λ_i and auxiliary polynomial B_i are determined. Where
 5 it is desired to rotate the values of B_i through register 55, second delay register 56 is bypassed. On the other hand, where it is desirable to utilize a previously calculated value of B_i , as indicated in the aforementioned algorithm, the value of B_i is directed into second delay register 56.

Continuing in Figure 3, calculation of the magnitude polynomial will be described. At
 10 the completion of $2t$ iterations as described above, register 52 will contain values S_4 - S_8 . In essence, determination of the magnitude polynomial can be modeled as $M(x) = \Lambda(x) S(x) \bmod x^{2t}$, in which the multiplication will be truncated after the $2t$ term. Indeed, only t terms need be determined under the assumption that no uncorrectable error was encountered. During the final iterations of the calculation of the error locator polynomial,
 15 register 52 is loaded with zeros such that, at the completion of $2t$ iterations, all storage locations in register 52 contain a zero value. After $2t$ iterations, the values in register 51 will be restored to their original positions, register 52 will contain all zero values and register 54 will contain the error locator polynomial, Λ_i . In a manner similar to the computation of the locator polynomial coefficients, the error magnitude coefficients are calculated iteratively. After t
 20 iterations, S_0 will be at the logical bottom of register 52 and Λ_0 at the logical bottom of register 54. At the completion of $t+1$ iterations, the product of multiplier 57 will be $S_0 \Lambda_0$, the first term of the error magnitude polynomial. The output of adder 59 is directed to the logical top of register 55, which now will be used to build the magnitude polynomial. After iteration $t+2$, syndrome value S_0 will be aligned with locator value Λ_1 , giving the product $S_0 \Lambda_1$; syndrome
 25 value S_1 will be aligned with Λ_0 , giving the product $S_1 \Lambda_0$; the summation of which giving $S_0 \Lambda_1 + S_1 \Lambda_0$, which is the second term of the error magnitude polynomial. This process will continue until all values of $M(x)$ are so determined. At iteration $2t$, all of the coefficients for the error magnitude polynomial will have been calculated. At this point, data flow of the error locator polynomial in register 54 and the error magnitude polynomial in register 55 can be
 30 directed out of solver 50.

Figure 4 illustrates one embodiment of a circular syndrome generator 70 that can be employed as register 51 in Figure 3, modified to accommodate an error correcting capability of $t=8$. Figure 5 is an embodiment 72 of one of the individual registers 71 in circular syndrome generator 70 in Figure 4. Although a circular syndrome generator is shown, it is by no means
 35 the only form of syndrome generator that can be employed as register 51.

The foregoing merely illustrates the principles of the invention, and it will thus be appreciated that those skilled in the art will be able to devise various alternative arrangements

1 which, although not explicitly described herein, embody the principles of the invention within
the spirit and scope of the following claims.

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1 What is claimed is:

1. A method for decoding an algebraic-coded message, comprising the steps of:
a. determining a discrepancy indicator;
5 b. determining an error locator polynomial according to an algorithm from a
selected class of decoding algorithms wherein an uncorrectable message is detected; and
c. producing a perceptible indication of the detected uncorrectable message.

2. The method of claim 1 wherein the selected class of decoding algorithms is a
10 Berlekamp-Massey algorithm.

3. The method of claim 2 wherein the Berlekamp-Massey algorithm is an iterative
algorithm.

4. The method of claim 3 wherein the iterative algorithm further includes the step
15 of evaluating the error locator polynomial for the presence of an uncorrectable message after
an iteration.

5. An apparatus for decoding an algebraic-coded message, comprising:
20 a. a plurality of storage devices, selected ones of the storage devices being
recirculating storage devices;
b. a plurality of arithmetic components operably connected with the plurality of
storage locations, the arithmetic components being operative within a Galois field; and
c. an uncorrectable message detector, operably connected with the storage devices
25 and the arithmetic components.

6. The apparatus of claim 5 wherein one of the recirculating storage devices is one
of a recirculating syndrome polynomial storage device, a recirculating error location polynomial
storage device, and an auxiliary coefficient storage device.
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7. The apparatus of claim 5, further comprising a syndrome generator.

8. The apparatus of claim 7 wherein the syndrome generator is a circular syndrome
generator.
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9. The apparatus of claim 8 wherein the circular syndrome generator is a
recirculating circular syndrome generator.

1 10. The apparatus of claim 6 wherein the one of a recirculating syndrome polynomial
storage device, a recirculating error location polynomial storage device, and an auxiliary
coefficient storage device, is an area-efficient device.

5 11. An apparatus for decoding an algebraic-coded message, comprising a circular
syndrome generator.

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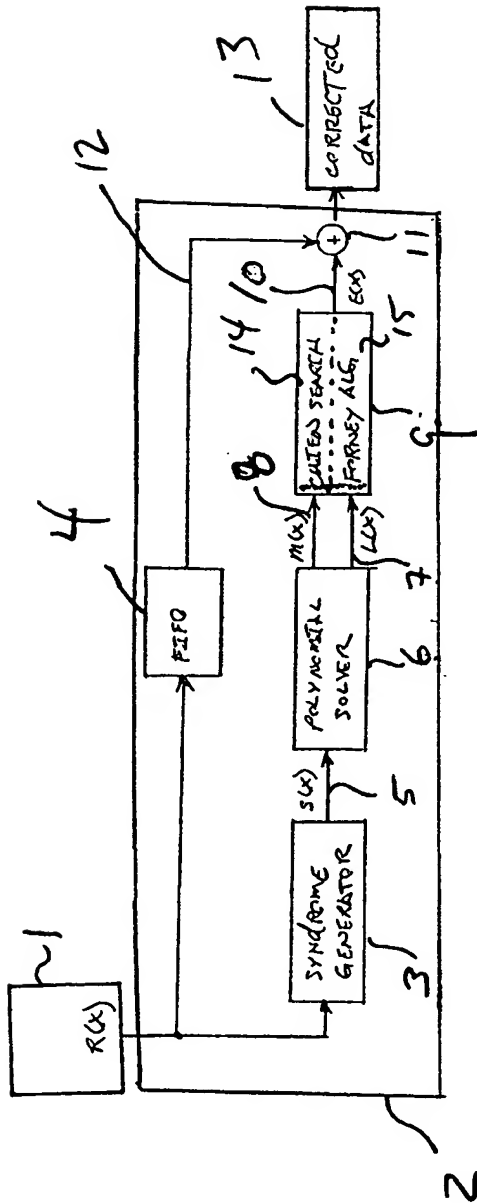
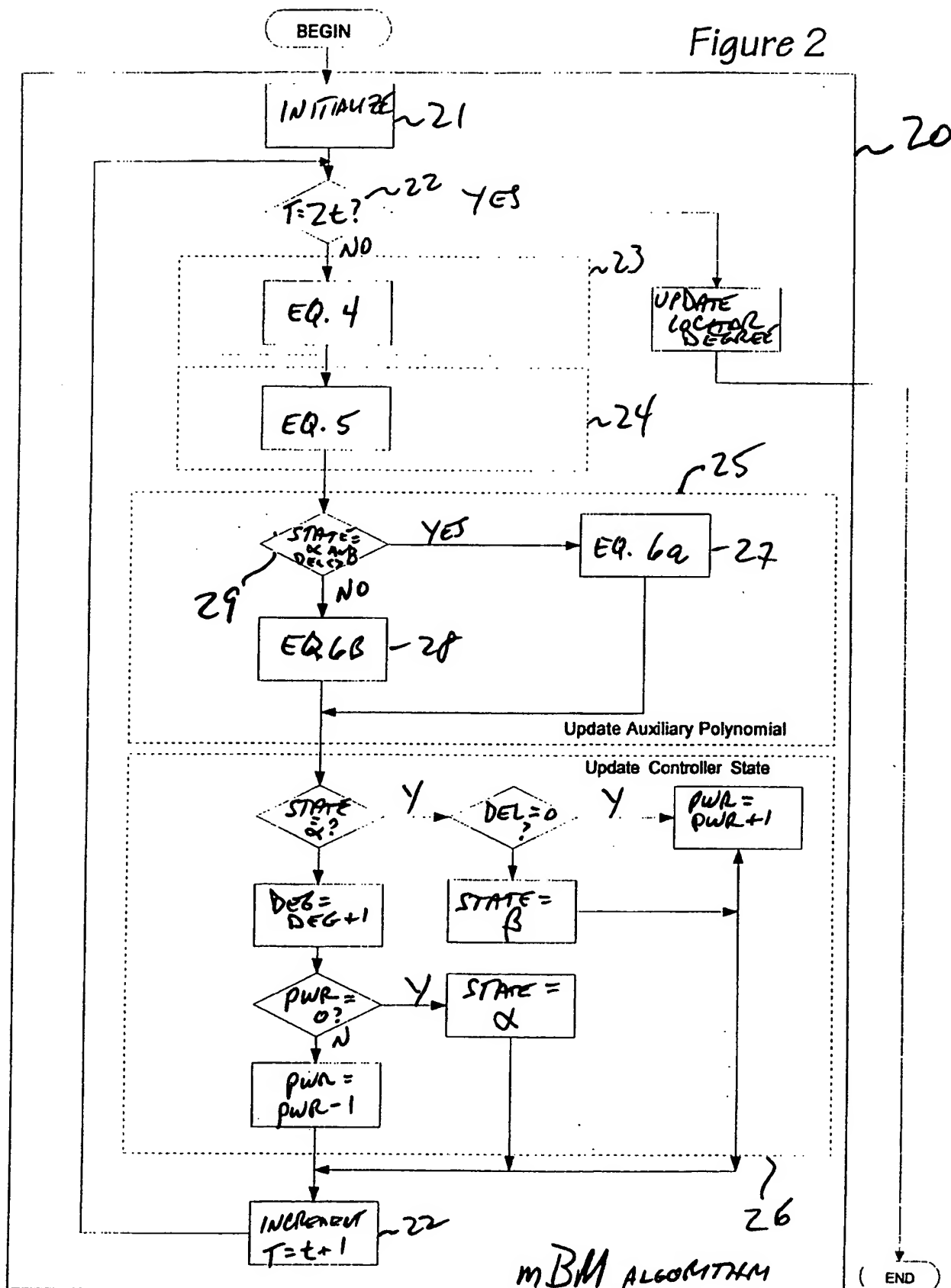


FIGURE 1

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Figure 2



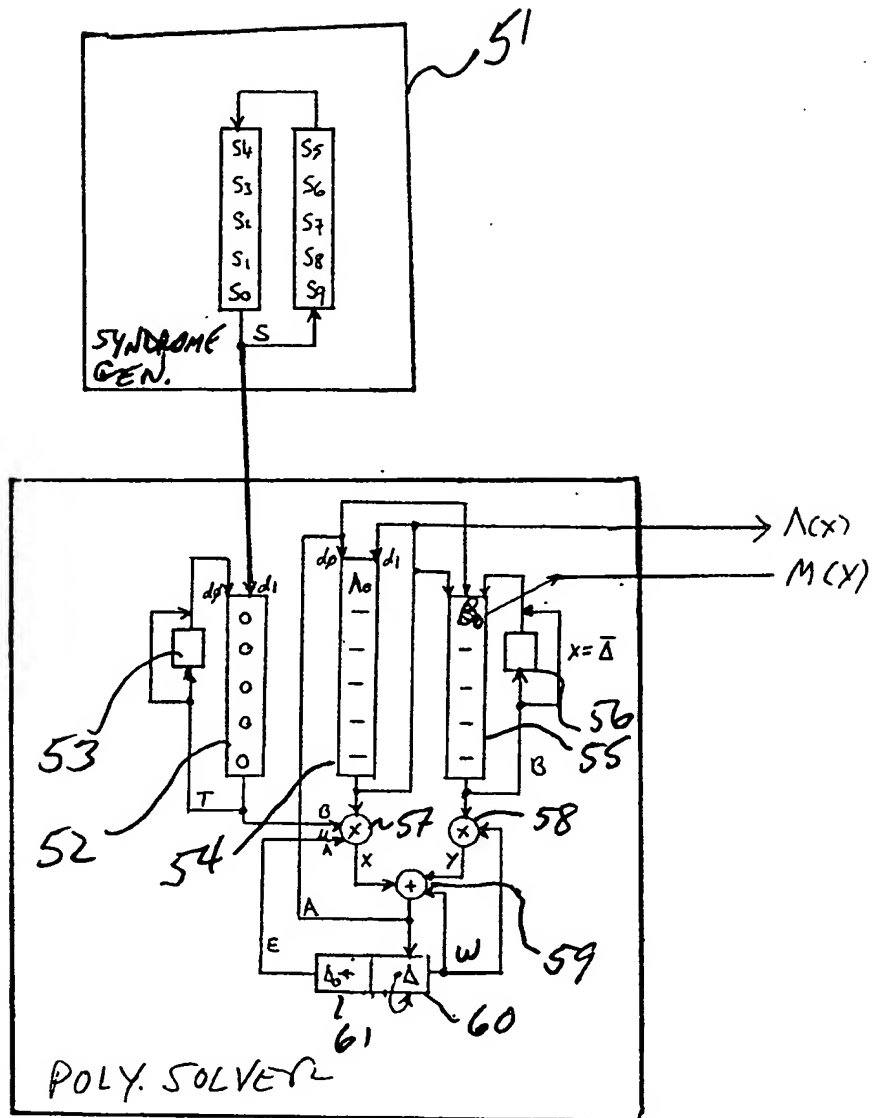


FIGURE 3

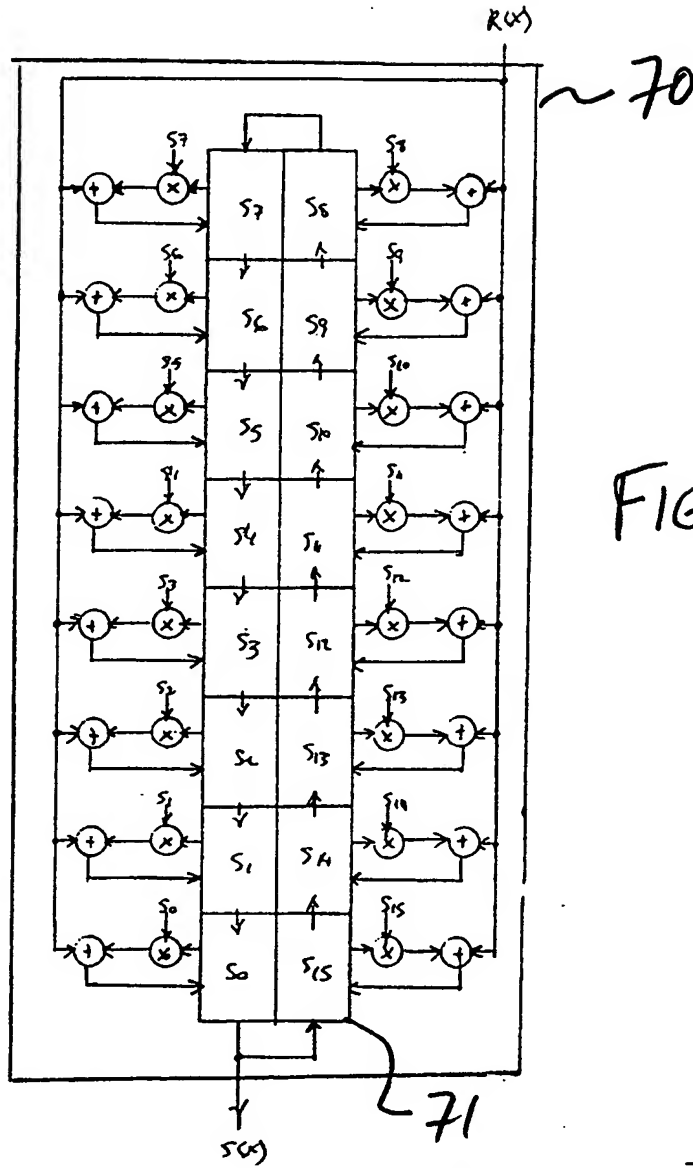
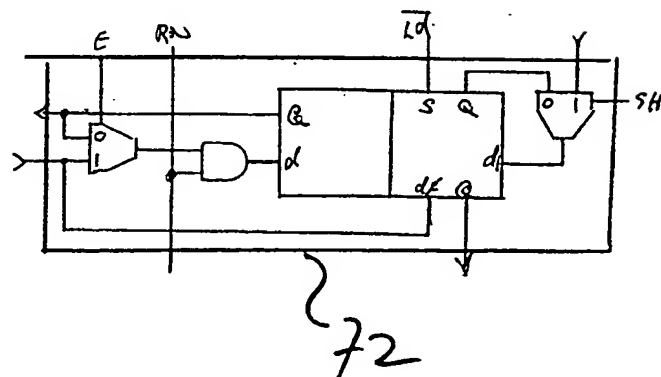


FIG. 5



INTERNATIONAL SEARCH REPORT

Intern. Appl. No.

PCT/US 99/26554

A. CLASSIFICATION OF SUBJECT MATTER
IPC 7 H03M13/15

According to International Patent Classification (IPC) or to both national classification and IPC

B. FIELDS SEARCHEDMinimum documentation searched (classification system followed by classification symbols)
IPC 7 H03M

Documentation searched other than minimum documentation to the extent that such documents are included in the fields searched

Electronic data base consulted during the international search (name of data base and, where practical, search terms used)

C. DOCUMENTS CONSIDERED TO BE RELEVANT

Category *	Citation of document, with indication, where appropriate, of the relevant passages	Relevant to claim No.
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Y	BLAHUT E.R.: "theory and practice of error control codes" 1984, ADDISON-WESLEY PUBLISHING COMPAGNY , LONDON XP002131806 page 176, paragraph 7.4 -page 178 page 191, paragraph 7.6 -page 193 -/-	1-4

☒ Further documents are listed in the continuation of box C.☒ Patent family members are listed in annex.

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Date of the actual completion of the international search

1 March 2000

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PCT/US 99/26554

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